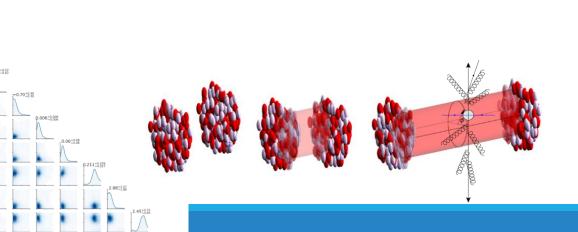


Hydrodynamics and Bayesian Inferences in isobar collisions

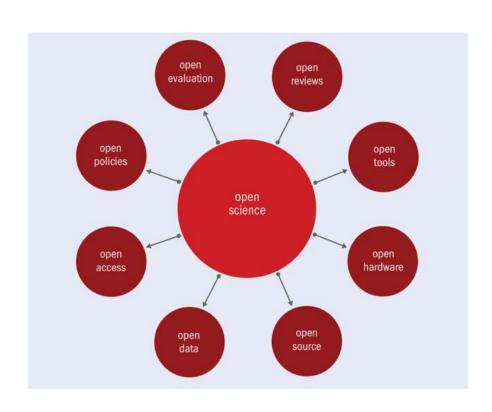
Latest Trajectum results on Isobar collisions

Based on 2112.13771 with Govert Nijs

Big thanks to STAR for sharing their data at very early stage



Wilke van der Schee BNL (virtual non-public workshop) 26 January 2022



A non-public workshop

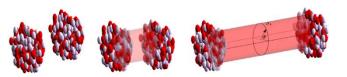
A discussion should be had if a workshop can be closed to the public

- Workshop hardly advertised, complicated to register
- Not ideal for transparent research, towards open science

Different but similar issue for large conferences (e.g. QM)

- A hefty fee may be realistic in terms of cost, but does not align with letting everyone participate (developing countries, students or general public)
- We should not repeat mistakes with journals: journals should be open access, as should zoom links
- Publicly funded science should be publicly available

Standard model of heavy ion collisions



(# parameters)

Trajectum

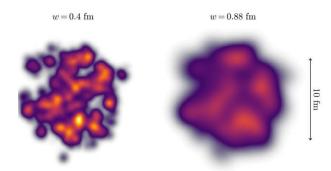
- New public heavy ion code
- Originally Utrecht (now MIT/CERN)
- Fast
- Precise (all cuts equal to experiment)
- Scalable



Roman excavations in Utrecht in 1929

Initial stage (9)

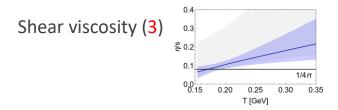
Subnucleonic structure? (7)

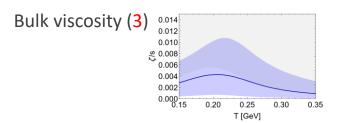


Non-thermal flow? (2) with varying speed (new)

Fluctuations? (1)

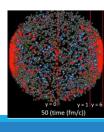
Viscous hydrodynamics (9)



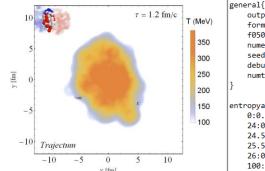


Second order transports: 3 (new)

Cascade of hadrons (1)

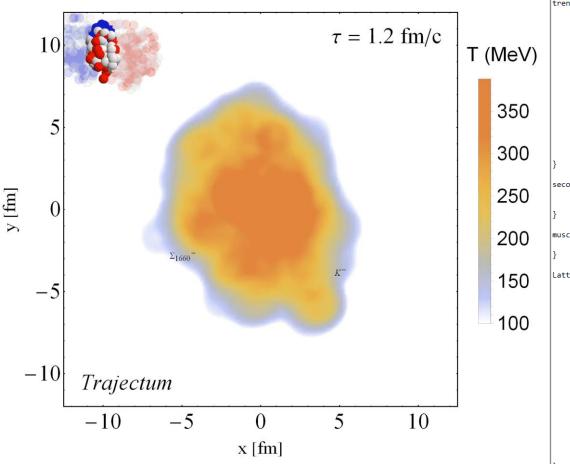


Trajectum



 Quite straightforward to use (see param file, right)

- 2. Includes analyse routine
 - Parallelised: can analyse unlimited number of events

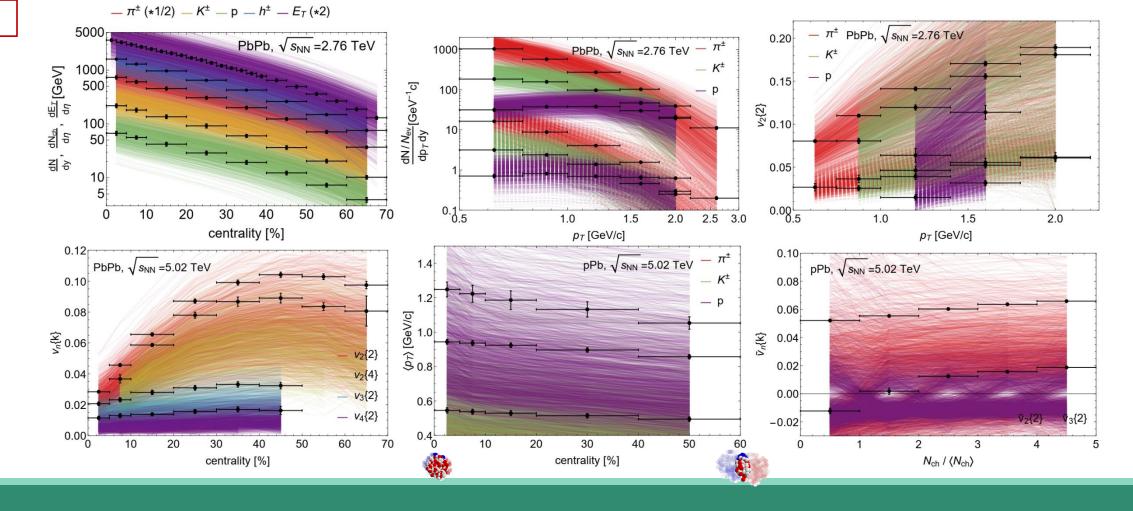


```
entropyacceptanceprobability{
   24:0.0
   24.5:0.05
   25.5:0.05
   26:0.0
   100:0.0
trentosubstructurePbPb{
   dmin=0.63933
   w=0.701919
   sigmann=70.0
   sigmafluct=0.73579
   p=0.14388
   q=1.0
   Eref=0.2
   norm=23.507
   freestreamingreferencetime=1.1708
   freestreamingvelocity=0.62672
   weaktostrong=0.0
   nref=20
   alpha=0
   nc=3.2747
   voverw=0.4892041602706295
secondorderhydro{
   numlatticesites=166.0
   latticesize=33.2
musclsolverktminmodfastmidpoint{
   cflconstant=0.08
LatticeEOStempdepDuke{
   shearhrg=0.0895066
   shearmin=0.0895066
   shearslope=0.43252
   shearcry=0.231195
   shearrelaxationtime=6.318855
   bulkmax=0.0030138
   bulkT0=0.21471
   bulkwidth=0.10906
   bulkrelaxationtime=0.0687
   deltapipiovertaupi=1.33333333333333
   phi7overpressure=0.128571
   taupipiovertaupi=1.61033
   lambdapiPiovertaupi=1.2
   deltaPiPiovertauPi=0.666666666
   lambdaPipiovertauPi=1.6
   phi1overpressure=0
   phi3overpressure=0
   phi6overpressure=0
cooperfryehadronizer{
   freezeouttemp=153.456
   rapidityrange=0.1
```

output=out format=smash f0500=false numevents=1 seed=7398984.747399307 debugoutput=true

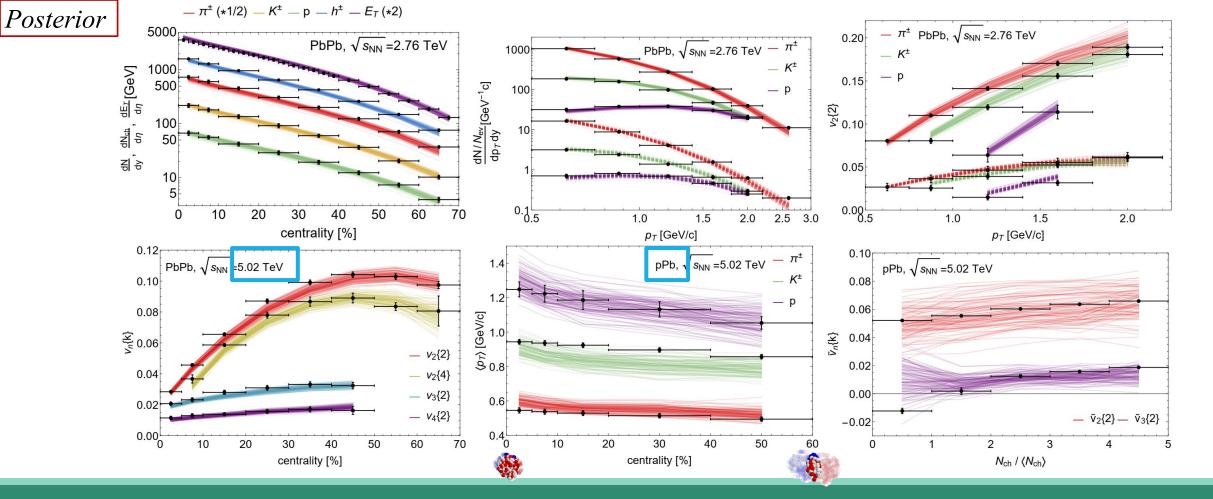
numthreads=2

Prior



Experimental observables: a wealth of data

- 1. Yields, spectra, identified $v_n\{2\}$ versus p_T , pPb and PbPb (514 datapoints)
- 2. First study with a comprehensive analysis including p_T -differential observables



Experimental observables: a wealth of data

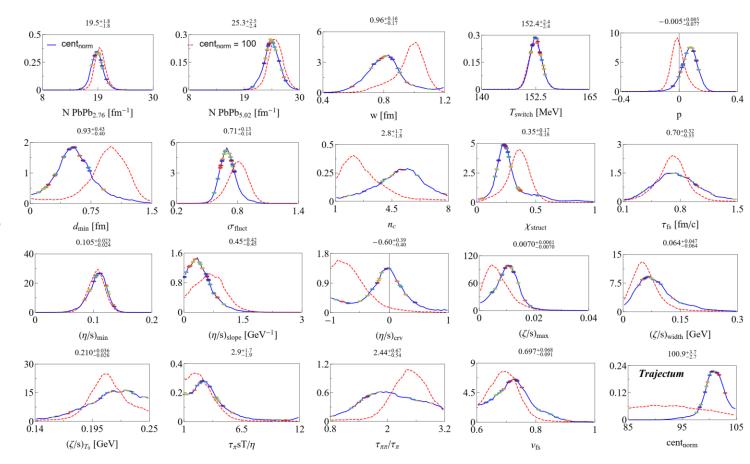
- 1. Yields, spectra, identified $v_n\{2\}$ versus p_T , pPb and PbPb (514 datapoints)
- 2. First study with a comprehensive analysis including p_T -differential observables

Posterior distributions

- Dashed: standard cent_{norm}
 - Emulation effects for cent_{norm} itself
- 2. Solid: posterior distributions
 - More accurate than previously

Also indicated: 20 randomly drawn points

- -> allows for systematic uncertainties
- This work: take MAP

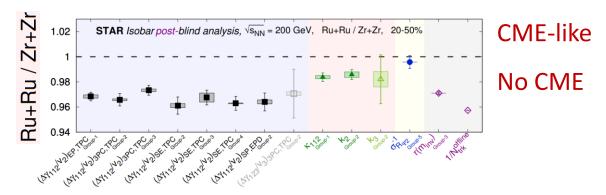


Isobar collisions at STAR

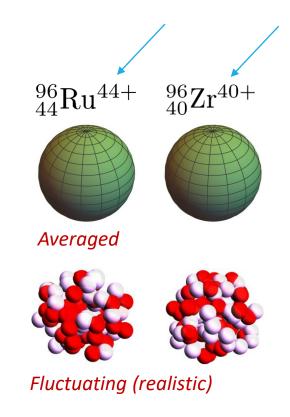
Varying the magnetic field

Idea: similar nuclei (same # of baryons), different charge

- Ruthenium generates a 10% larger magnetic field
- Ideal set-up to suppress background and detect Chiral Magnetic Effect (CME)
- Very precise blinded analysis by STAR:



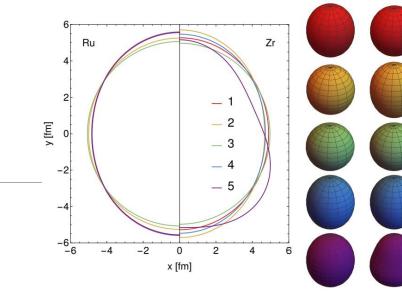
Unfortunately (?), no CME detected



Isobar collisions at STAR

Five different cases simulated:

nucleus	R_p [fm]	$\sigma_p [\mathrm{fm}]$	R_n [fm]	σ_n [fm]	eta_2	eta_3	$\sigma_{\mathrm{AA}}\left[\mathrm{b}\right]$
$^{96}_{44} Ru(1)$	5.085	0.46	5.085	0.46	0.158	0	4.628
$^{96}_{40}\mathrm{Zr}(1)$	5.02	0.46	5.02	0.46	0.08	0	4.540
$^{96}_{44} Ru(2)$	5.085	0.46	5.085	0.46	0.053	0	4.605
$^{96}_{40}\mathrm{Zr}(2)$	5.02	0.46	5.02	0.46	0.217	0	4.579
$^{96}_{44}$ Ru(3)	5.06	0.493	5.075	0.505	0	0	4.734
$^{96}_{40}\mathrm{Zr}(3)$	4.915	0.521	5.015	0.574	0	0	4.860
$^{96}_{44}$ Ru(4)	5.053	0.48	5.073	0.49	0.16	0	4.701
$^{96}_{40}\mathrm{Zr}(4)$	4.912	0.508	5.007	0.564	0.16	0	4.829
$^{96}_{44}$ Ru(5)	5.053	0.48	5.073	0.49	0.154	0	4.699
$^{96}_{40}\mathrm{Zr}(5)$	4.912	0.508	5.007	0.564	0.062	0.202	4.871



- e-A scattering experiments(STAR case 1)
- 2. Theory (finite-range liquid drop model, STAR 2)
- 3. DFT with neutron skin (spherical) [1]
- DFT with neutron skin (deformed, $\beta_2 = 0.16$) [1]
- As 4, but with β_2 from electric transition probability and β_3 from comparing AMPT with STAR [2]

For each case we run 0.5M collisions except for case 5 (5M), 14M in total.

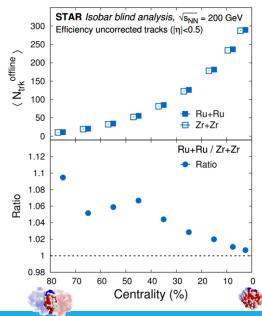
Isobar collisions at STAR - Multiplicity

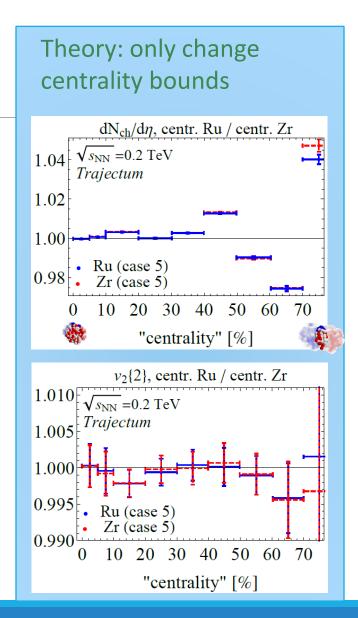
Precision and non-conventional definition of centrality

Subtlety in STAR data: "centrality label" is different for Ru and Zr

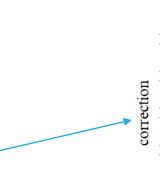
- Especially important for multiplicity (~7% effect)
- Hardly significant for other observables (<0.5% for v₂)

Centrality	7	Ru+Ru		Zr+Zr			
label (%)	Centrality(%)	$N_{ m trk}^{ m offline}$	$\langle N_{ m trk}^{ m offline} angle$	Centrality(%)	$N_{ m trk}^{ m offline}$	$\langle N_{ m trk}^{ m offline} angle$	offline
0–5	0-5.01	258500.	289.32	0-5.00	256500.	287.36	
5 - 10	5.01 - 9.94	216258.	236.30	5.00 – 9.99	213256.	233.79	
10 - 20	9.94 – 19.96	151216.	181.76	9.99-20.08	147213.	178.19	
20 – 30	19.96-30.08	103151.	125.84	20.08 - 29.95	100147.	122.35	
30 – 40	30.08-39.89	69103.	85.22	29.95 – 40.16	65100.	81.62	
40 – 50	39.89-49.86	4469.	55.91	40.16 – 50.07	4165.	52.41	
50 – 60	49.86-60.29	2644.	34.58	50.07 - 59.72	2541.	32.66	
60 - 70	60.29 – 70.04	15.=26.	20.34	59.72-70.00	1425.	19.34	
70 – 80	70.04 – 79.93	815.	11.47	70.00-80.88	714.	10.48	1
20-50	19.96-49.86	44151.	89.50	20.08 – 50.07	41147.	85.68	
20-30 30-40 40-50 50-60 60-70 70-80	19.96–30.08 30.08–39.89 39.89–49.86 49.86–60.29 60.29–70.04 70.04–79.93	69103. 4469. 2644. 1526. 815.	125.84 85.22 55.91 34.58 20.34 11.47	20.08–29.95 29.95–40.16 40.16–50.07 50.07–59.72 59.72–70.00 70.00–80.88	65100. 4165. 2541. 1425. 714.	122.35 81.62 52.41 32.66 19.34 10.48	





Isobar collisions at STAR - Multiplicity

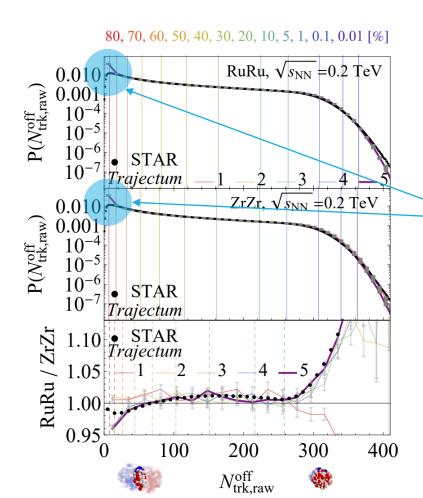


Wilke van der Schee, CERN

AuAu @ 200 GeV

 $dN_{ch}/d\eta$

 $N_{\rm ch}/{\rm raw}~N_{\rm ch}~[0808.2041]^{-1}$

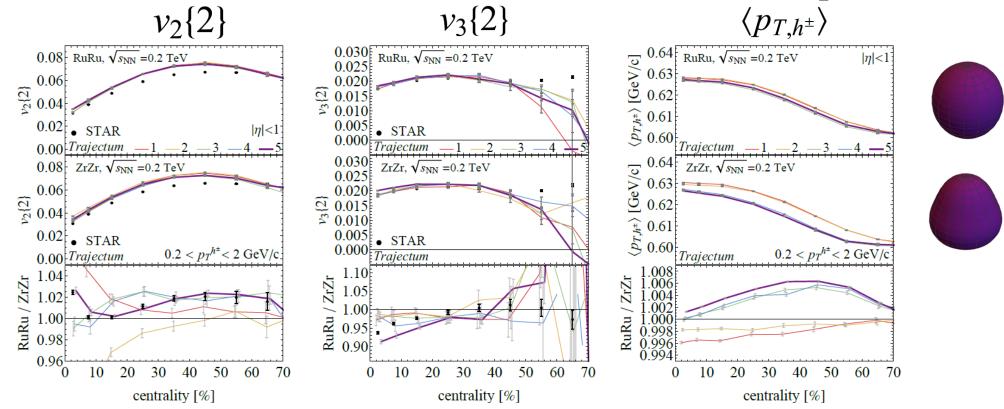


Better to directly look at (raw) data

- Experimental subtlety: crucial to correct for detector efficiency
- Trajectum subtlety: norm not fitted to RHIC energy: multiply mult by 1.21
- Experiment misses (many) very peripheral collisions:
 multiply P(N) by 1.31 to correct for this (not for ratio)
- Ratio experiment: normalise both and divide Subtle: experiment unreliable for $N_{trk} < 50$ Ratio theory: integrate **Ru+Zr experiment and Ru+Zr theory** for $N_{trk} > 50$ and require ratio to match Exp-theory comparison only depends on $N_{trk} > 50$

Only case 3, 4 and 5 match well over entire range (neutron-skin)

Isobar collisions at STAR – Flow and mean p_T



Statistics better for best case (5, with 5M collisions)

- Excellent fit, especially for v2 ratio, v3 ratio overestimated at central
- Note that *Trajectum* is not fitted to RHIC energies, no absolute agreement
- Mean transverse momentum is a prediction

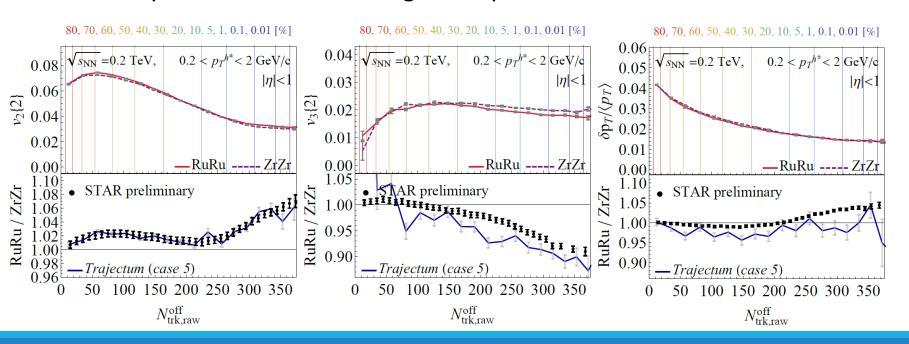
RuRu

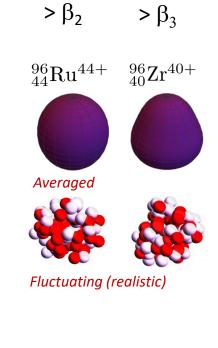
ZrZr

Extremely ultracentral collisions

Going to 0.01% centrality (we sample from 250M Trento events)

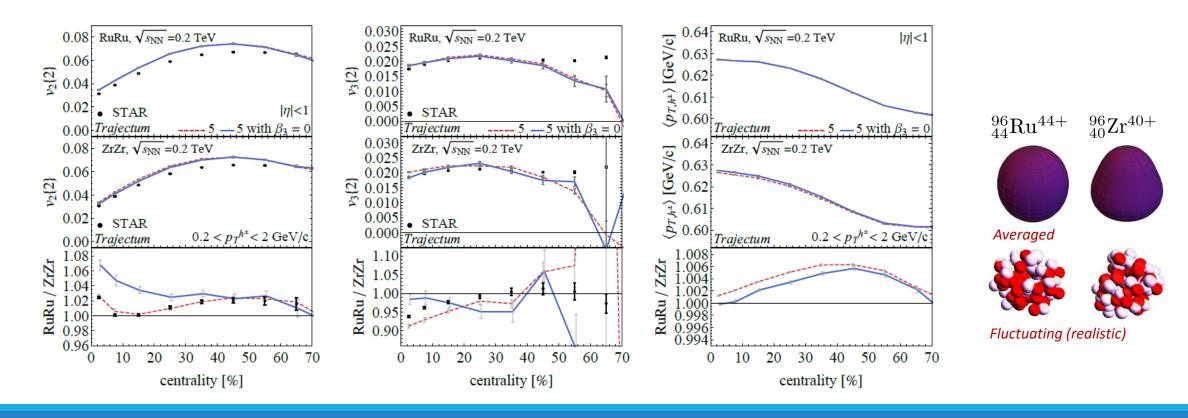
- Excellent match v2, v3 en pt fluct somewhat overpredicted
- Extremely ultracentral is ideal regime to probe nuclear structure





Effect of β_3 on observables

Clear effect on v_3 , but also on v_2 . Need a (Bayesian) refit of β_2 as well to fit v_2 and v_3 ?



Initial state predictors

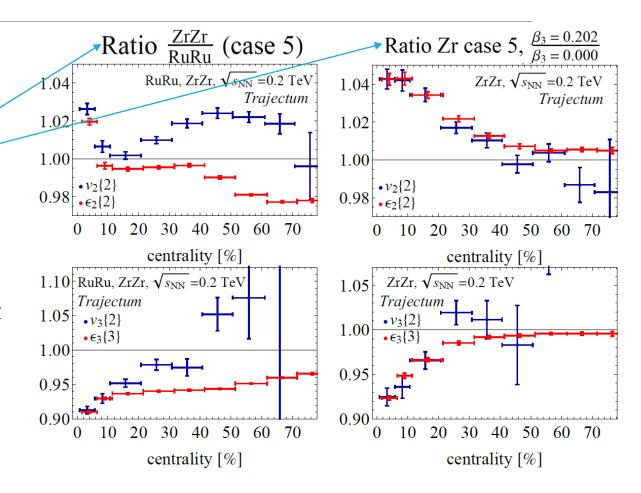
With large sample we can verify the relation

$$v_n\{2\} = \kappa \epsilon_n\{2\}$$

All else being equal this works, e.g. within Zr as in right plots

If also size changes etc (Zr vs Ru), it can affect κ and the initial geometry cannot be used

Unfortunate: hydro is expensive...



Discussion

Isobar collisions: an opportunity at unprecedented precision

- So many systematics cancel, both experimentally and in theory
- Implies a need for statistics... of order 1M events at least to be competitive

A Bayesian point of view

- So far only performed a scan of several Wood-Saxon parameters (see also [1, 2])
- Global analysis would be preferred, but statistically hard to pull off
- Initial state predictor would be ideal, but first tests are not encouraging

Towards magnetic effects

- First things first: understanding nuclear structure. Interesting in itself (!), see also neutron stars
- Trajectum done without 3+1D or baryon number...
- Isobars still ideal setting to probe magnetic effect, but will take time to have theory at required precision

